

Causal Inference (What If)

Ch11 Why models?

이종진

Seoul National University

ga0408@snu.ac.kr

August 05, 2021

Ch 11, Why model?

- ▶ Part II (ch11 ~ 18) is about the parametric (model-based) estimators.
- ▶ This chapter motivates the need for models in data analysis
- ▶ "Data cannot always speak for themselves, rather we need to supplement the data with a model."

Necessity of model; example

▶ Example

- 16 individuals infected with HIV.
- A continuous outcome Y (CD4 cell count)
- Wish to estimate the mean of Y among individuals with treatment level

$$A = a$$

- Conditional mean, $E(Y|A = a)$

▶ Treatment A could be

- a dichotomous variables with two possible values
- a polytomous variables with 4 possible values
- a integer values from 0 to 100mg

Necessity of model; example

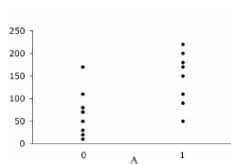


Figure 11.1

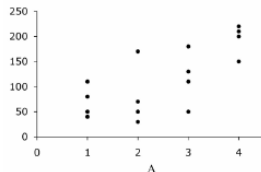


Figure 11.2

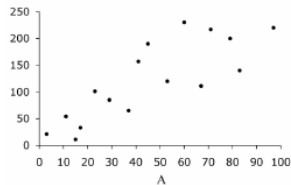


Figure 11.3

- ▶ # of possible values of $A >$ # of observed individuals
- ▶ How can we estimate the mean of outcome Y among individuals with treatment level $A = 90$ which not observed?

Necessity of model; example

- ▶ We often need to supplement the data with a model.
- ▶ With a priori restrictions, model can compensate for the lack of sufficient information in the data.
- ▶ $E(Y|A = a) = \theta_0 + \theta_1 A$

Nonparametric & parametric

$$E(Y|A) = \theta_0 + \theta_1 A$$

▶ Nonparametric estimators

- Treatment A is a dichotomous; 2 quantities and 2 parameters
- Without any a priori restrictions,
- Standardization, IP weighting, stratification and matching.

▶ Parametric estimators

- Treatment A takes integer values; 101 quantities and 2 parameters
- Impose a priori restrictions on conditional mean (linear)

Smoothing & The bias-variance trade-off

▶ Smoothing

- Linear model can be more flexible, introducing $A^2 \dots, A^{15}$
- The curve generally becomes more "wiggly", or less smooth, as the number of paramters increase.

▶ The bias-variance trade-off

- The larger the number of paramters in model, the more protection afforded against bias from the model misspecification.
- Although less smooth models may yield a less biased estimate, they also result in larger variance.